

Believe It or Not – Adding belief annotations to databases

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<http://db.cs.washington.edu/beliefDB/>

High-level overview

- DBMS: manage consistent data
- Applications need inconsistent DM
 - Scientific databases reason: disagreement !
 - Internet community databases
- Community DBMS: manage inconsistent views

- This work: **Belief databases**
 - manage data and curation
 - grounded in modal and default logic
 - implemented on top of relational model

Agenda

- Motivating example
- Logic foundations
- Relational implementation
- Discussion

Motivating application

- NatureMapping project (<http://depts.washington.edu/natmap/>)
 - volunteer contribute animal observations
 - one person curates the database

problem: does not scale!

Observations

| <u>id</u> | uid | species | date | location | comment |
|-----------|-------|---------|----------|-------------|----------------|
| 2 | Alice | Crow | 06-14-08 | Lake Placid | found feathers |

Sightings (S)

| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Crow | 06-14-08 | Lake Placid |

Comments (C)

| <u>cid</u> | comment | sid |
|------------|----------------|-----|
| c1 | found feathers | s2 |

1. Distinct database instances



Alice

S

| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Crow | 06-14-08 | Lake Placid |



Bob

S

| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Raven | 06-14-08 | Lake Placid |

D1: Belief worlds: individually consistent,
mutually possibly inconsistent

1. Distinct database instances



Alice

S

| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Crow | 06-14-08 | Lake Placid |



Bob

S

| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Raven | 06-14-08 | Lake Placid |

BeliefSQL

I: Alice believes that she saw a crow.

```
insert into BELIEF 'Alice' Sightings
values ('s2','Alice','Crow','06-14-08','Lake Placid')
```

I: Bob believes that she actually saw a raven.


```
insert into BELIEF 'Bob' Sightings
values ('s2','Alice','Raven','06-14-08','Lake Placid')
```

Q: Who believes something different than Alice and what?

```
select U2.name, S1.species, S2.species
from Users as U,
BELIEF 'Alice' Sightings as S1,
BELIEF U.uid Sightings as S2,
where S1.sid = S2.sid
and S1.species <> S2.species
```

A: {'Bob', 'Crow', 'Raven'}

2. Open world assumption



Alice

S

| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Crow | 06-14-08 | Lake Placid |



Bob

S

| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Raven | 06-14-08 | Lake Placid |



Carol

S

| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Crow | 06-14-08 | Lake Placid |
| s2 | Alice | Raven | 06-14-08 | Lake Placid |


⊖

⊖

Adapted key constraints !

D2: Model incomplete knowledge with explicit negative beliefs

2. Open world assumption



Alice


s

| sid | uid | specie |
|-----|-------|--------|
| s2 | Alice | Crow |

I: Carol does not believe that Alice saw a crow nor a raven.

```

insert into BELIEF 'Carol' not Sightings
values ('s2','Alice','Crow','06-14-08','Lake Placid')
insert into BELIEF 'Carol' not Sightings
values ('s2','Alice','Raven','06-14-08','Lake Placid')
    
```



Bob

s

| sid | uid | specie | date | location |
|-----|-------|--------|----------|-------------|
| s2 | Alice | Raven | 06-14-08 | Lake Placid |



Carol


s

| sid | uid | species | date | location |
|-----|-------|---------|----------|-------------|
| s2 | Alice | Crow | 06-14-08 | Lake Placid |
| s2 | Alice | Raven | 06-14-08 | Lake Placid |

⊖

⊖


2. Open world assumption



Alice

S

| sid | uid | species | date |
|-----|-------|---------|------|
| s2 | Alice | Crow | 06- |



Bob

S

| sid | uid | species | date |
|-----|-------|---------|------|
| s2 | Alice | Raven | 06- |



Carol

S

| sid | uid | species | date | location | |
|-----|-------|---------|----------|-------------|---|
| s2 | Alice | Crow | 06-14-08 | Lake Placid | ⊖ |
| s2 | Alice | Raven | 06-14-08 | Lake Placid | ⊖ |

Q: Who disagrees with a sighting from '06-14-08' that Alice believes?

```

select  U.name, S1.species
from    Users as U,
        BELIEF 'Alice' Sightings as S1,
        BELIEF U.uid not Sightings as S2
where   S1.sid = S2.sid
and     S1.uid = S2.uid
and     S1.species = S2.species
and     S1.date = '06-14-08'
and     S2.date = '06-14-08'
and     S1.location = S2.location
    
```

A: {('Bob', 'Crow'), ('Carol', 'Crow')}

3. Higher-order beliefs



Alice

S

| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Crow | 06-14-08 | Lake Placid |



Bob

S

| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Raven | 06-14-08 | Lake Placid |

C

| <u>cid</u> | comment | sid |
|------------|----------------------|-----|
| c1 | plain black feathers | s2 |



Bob


Alice

C

| <u>cid</u> | comment | sid |
|------------|-----------------------|-----|
| c1 | purple-black feathers | s2 |

D3: Beliefs about other user's beliefs: allow discussion between users

3. Higher-order beliefs




Alice

| S | <u>sid</u> | uid | species |
|---|------------|-------|---------|
| | s2 | Alice | Crow |

I: According to Bob, Alice believes that the feathers of the sighted animal were plain black.

insert into **BELIEF 'Bob'** **BELIEF 'Alice'** Comments values ('c1', 'plain black feathers', 's2')



Bob

| S | <u>sid</u> | uid | species | | |
|---|------------|-------|---------|----------|-------------|
| | s2 | Alice | Raven | 06-14-08 | Lake Placid |


| C | <u>cid</u> | comment | sid |
|---|------------|----------------------|-----|
| | c1 | plain black feathers | s2 |



Bob Alice


| C | <u>cid</u> | comment | sid |
|---|------------|-----------------------|-----|
| | c1 | purple-black feathers | s2 |

3. Higher-order beliefs



Alice

| S | sid | uid | specie |
|---|-----|-------|--------|
| | s2 | Alice | Crow |



Bob

| S | sid | uid | specie |
|---|-----|-------|--------|
| | s2 | Alice | Raven |


| C | cid | comment |
|---|-----|-----------------|
| | c1 | plain black fea |

Q: Which comments does Alice believe according to Bob, which he does not believe himself?

```

select  C1.cid, C1.comment
from    BELIEF 'Bob' BELIEF 'Alice' Comments as C1,
        BELIEF 'Bob' not Comments as C2
where   C1.cid = C2.cid
and     C1.comment = C2.comment
and     C1.sid = C2.sid
    
```

A: {{('c1','plain-black feathers')}}



Bob Alice

| C | cid | comment | sid |
|---|-----|-----------------------|-----|
| | c1 | purple-black feathers | s2 |

3. Higher-order beliefs



Alice

S

| sid | uid | species |
|-----|-------|---------|
| s2 | Alice | Crow |

Q: Which comments does Alice believe according to somebody, which (s)he does not believe themselves?

```

select  U.name, C1.sid, C1.comment
from    Users as U,
        BELIEF U.uid BELIEF 'Alice' Comments as C1,
        BELIEF U.uid not Comments as C2
where   C1.cid = C2.cid
and     C1.comment = C2.comment
and     C1.sid = C2.sid
    
```



Bob

S

| sid | uid | species |
|-----|-------|---------|
| s2 | Alice | Raven |

C

| cid | comment |
|-----|----------------------|
| c1 | plain black feathers |

where C1.cid = C2.cid
and C1.comment = C2.comment
and C1.sid = C2.sid



A: {'Bob', 'c1', 'plain-black feathers'}



Bob

Alice

C

| cid | comment | sid |
|-----|-----------------------|-----|
| c1 | purple-black feathers | s2 |



4. Message board assumption



Alice

S

| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Crow | 06-14-08 | Lake Placid |



Bob

S

| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Raven | 06-14-08 | Lake Placid |

C

| <u>cid</u> | comment | sid |
|------------|----------------------|-----|
| c1 | plain black feathers | s2 |



Bob

Alice

S


| <u>sid</u> | uid | species | date | location |
|------------|-------|---------|----------|-------------|
| s2 | Alice | Crow | 06-14-08 | Lake Placid |

C

| <u>cid</u> | comment | sid |
|------------|-----------------------|-----|
| c1 | purple-black feathers | s2 |


D4: Default assumption: models a trusting attitude & avoids repeated inserts

4. Message board assumption



Alice


| S | <u>sid</u> | uid | species |
|---|------------|-------|---------|
| | s2 | Alice | Crow |



Bob

| S | <u>sid</u> | uid | species |
|---|------------|-------|---------|
| | s2 | Alice | Raven |

| C | <u>cid</u> | comment |
|---|------------|----------------------|
| | c1 | plain black feathers |



Bob Alice

| S | <u>sid</u> | uid | species | | |
|---|------------|-------|---------|----------|-------------|
| | s2 | Alice | Crow | 06-14-08 | Lake Placid |

| C | <u>cid</u> | comment | sid |
|---|------------|-----------------------|-----|
| | c1 | purple-black feathers | s2 |

Q: Which animal sightings does Alice believe according to Bob, which he does not believe himself?

```

select  S1.sid, S1.species
from    BELIEF 'Bob' BELIEF 'Alice' Sightings as S1,
        BELIEF 'Bob' not Sightings as S2
where   S1.sid = S2.sid
and     S1.uid = S2.uid
and     S1.species = S2.species
and     S1.date = S2.date
and     S1.location = S2.location
    
```

A: {{'s2', 'Crow'}}

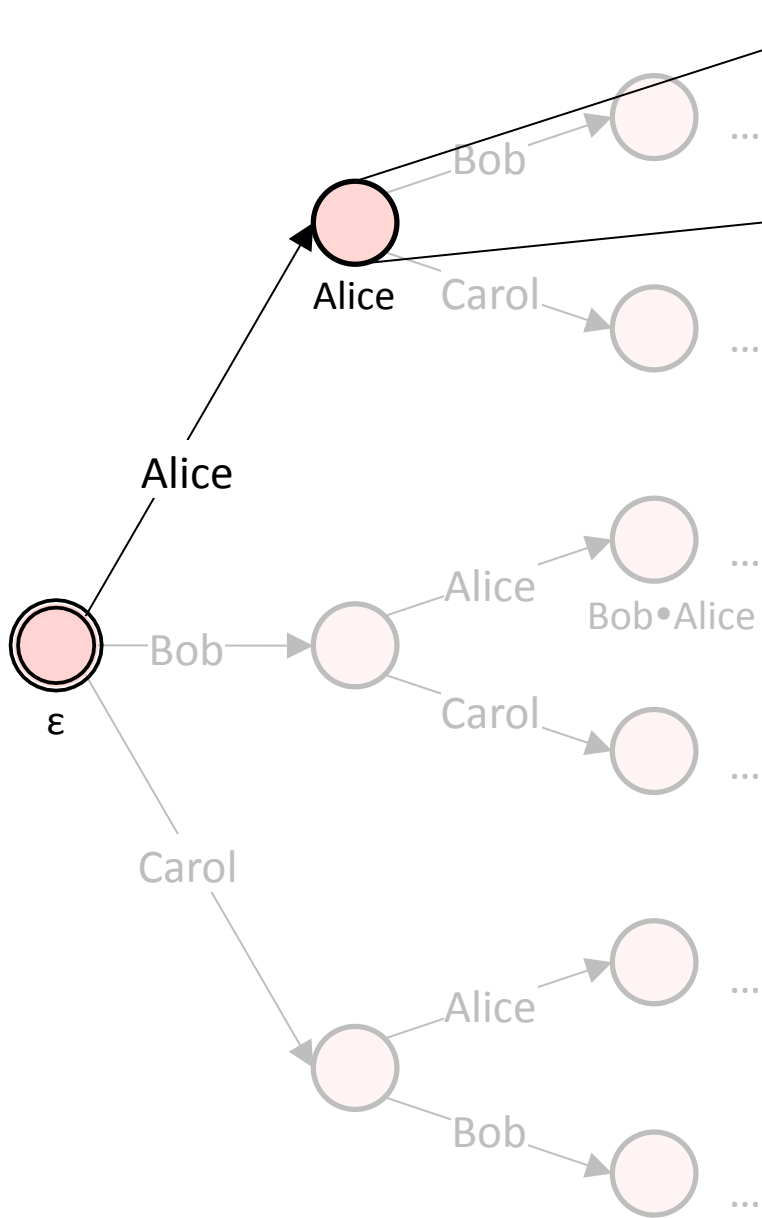
What we have seen so far

- 4 Design decisions for Belief Database model
 - Distinct belief worlds
 - Open world assumption (OWA)
 - Higher-order beliefs
 - Message board assumption
- **BeliefSQL**
 - SQL + 'BELIEF' (+ 'not')

Agenda

- Motivating example
- **Logic foundations**
- Relational implementation
- Discussion

Logic foundations: Belief statements



S

| sid | uid | species | ... |
|-----|-------|---------|-----|
| s2 | Alice | Crow | ... |

insert into **BELIEF 'Alice'** S
values ('s2', 'Alice', 'Crow',...)

$i: \square_{\text{Alice}} S^+(\text{'s2', 'Alice', 'Crow', ...})$

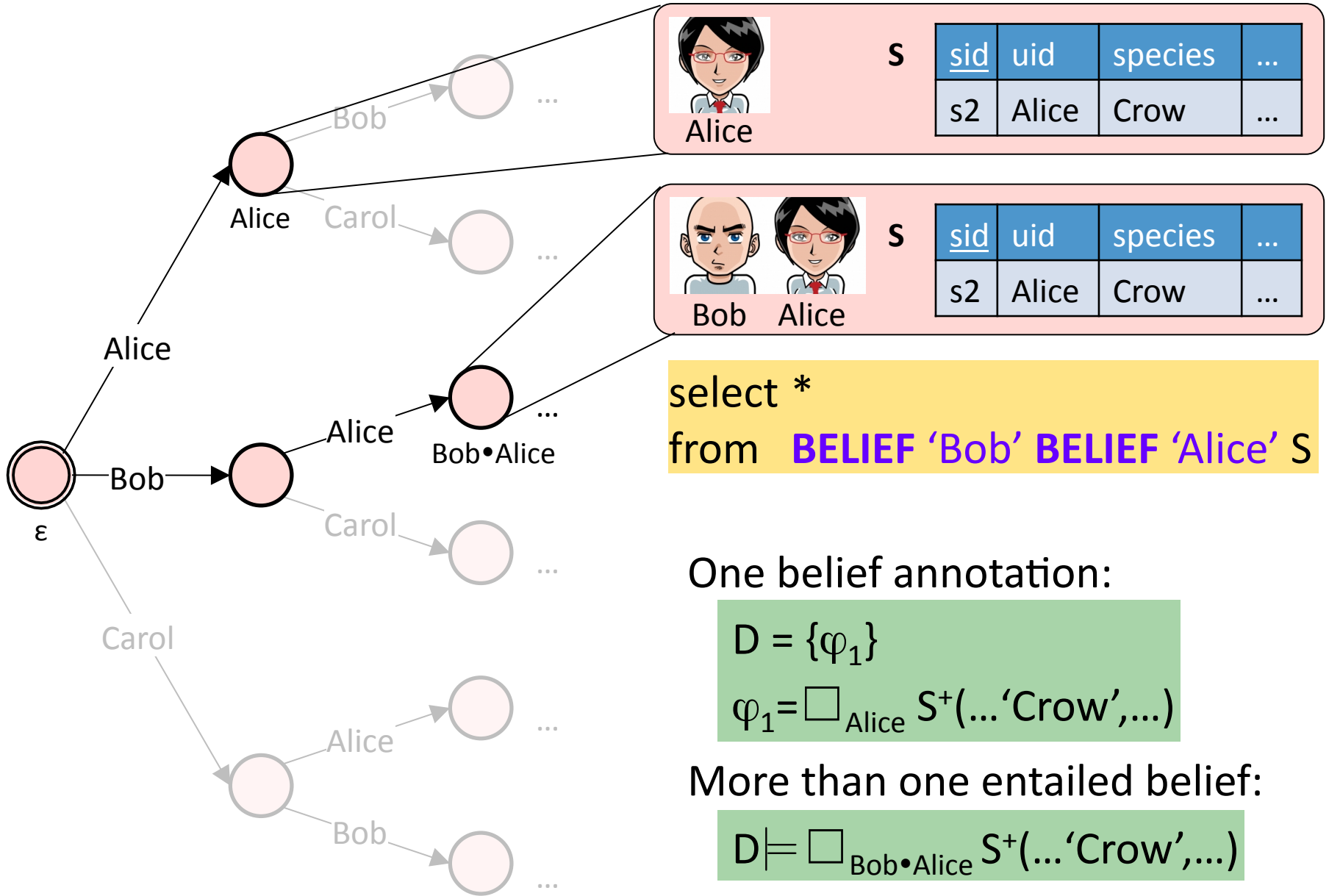
modal operator & belief path (w) relational tuple (t)
sign (s)

belief statement

$\varphi = \square_w t^s$ "annotation of ground tuple"

Belief database $D = \{\varphi_1, \dots, \varphi_n\}$

Logic foundations: Entailment



select *
from BELIEF 'Bob' BELIEF 'Alice' S

One belief annotation:

$$D = \{\varphi_1\}$$

$$\varphi_1 = \square_{\text{Alice}} S^+(\dots \text{'Crow'}, \dots)$$

More than one entailed belief:

$$D \models \square_{\text{Bob} \bullet \text{Alice}} S^+(\dots \text{'Crow'}, \dots)$$

Logic foundations: Message board assumption

Message board assumption

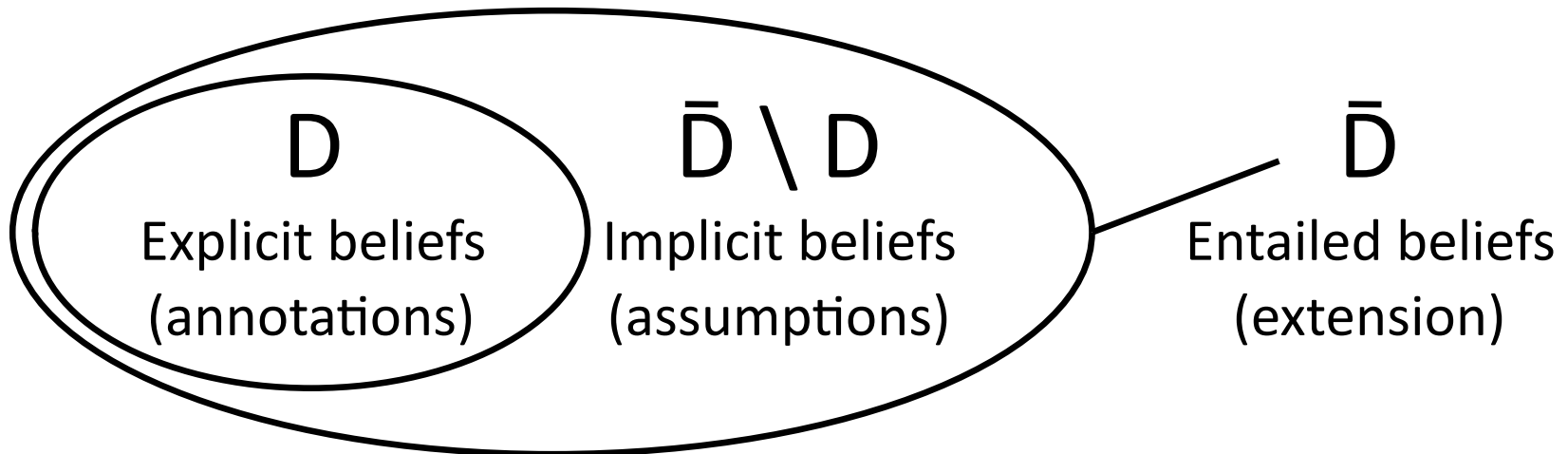
If $D \models \Box_w t^s$
and $\Box_{u \bullet w} t^s$ consistent with D
then $D \models \Box_{u \bullet w} t^s$



Default logic

$$\frac{\varphi : \Box_u \varphi}{\Box_u \varphi}$$

non-monotonic reasoning !



belief database “contains” more than the explicit belief annotations !

“Semi-formal” problem statement

INPUT

Belief statements

$$i_1: \varphi_1$$

$$i_2: \varphi_2$$

...

$$i_n: \varphi_n$$

Adapted key constraints

Message board assumption

$$\frac{\varphi : \Box_u \varphi}{\Box_u \varphi}$$

$$\Box_u \varphi$$

OUTPUT

$$D \models \varphi ?$$

$$D \models \Box_{w_1 \dots w_d} R^+(x_1, \dots, x_l) ?$$

$$q(\bar{x}) :- \Box_{\bar{w}} R_i^+(\bar{x}_i)$$

Belief Conjunctive Queries (BCQ)

$$q(\bar{x}) :- \Box_{\bar{w}_1} R_1^{s_1}(\bar{x}_1), \dots, \Box_{\bar{w}_g} R_g^{s_g}(\bar{x}_g)$$

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Canonical Kripke structure

Belief statements*

$i_1: s1_1^+$

$i_2: \square_{\text{Bob}} s1_1^-$

$i_3: \square_{\text{Bob}} s1_2^-$

$i_4: \square_{\text{Alice}} s2_1^+$

$i_5: \square_{\text{Alice}} c1_1^+$

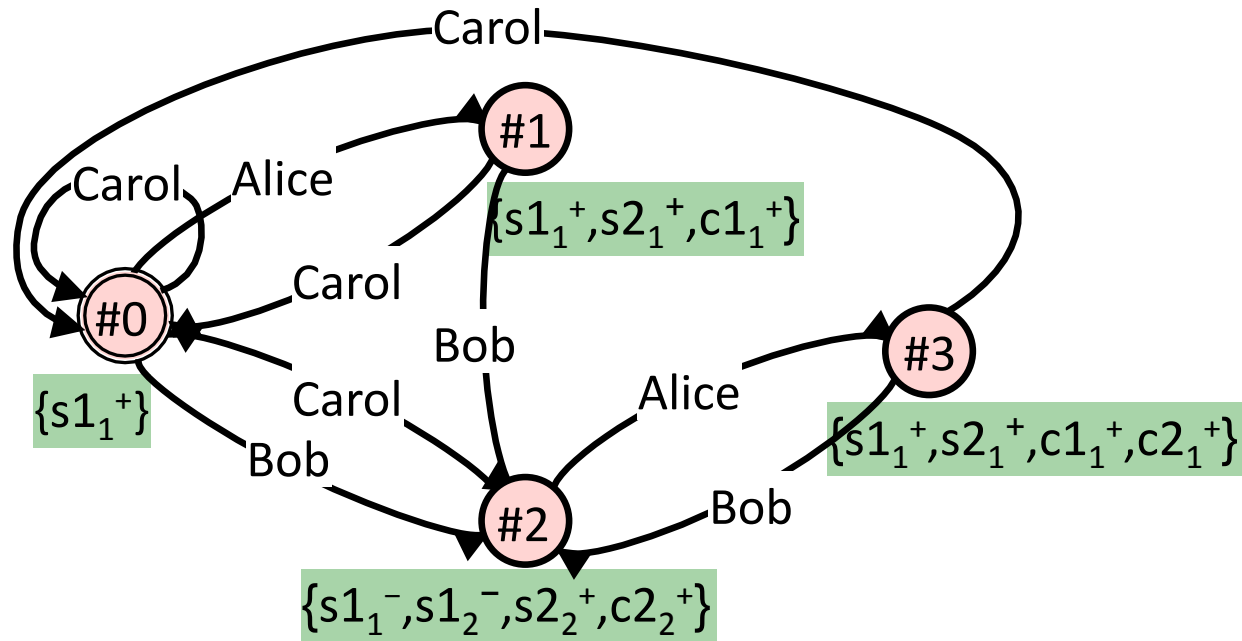
$i_6: \square_{\text{Bob}} s2_2^+$

$i_7: \square_{\text{Bob} \bullet \text{Alice}} c2_1^+$

$i_8: \square_{\text{Bob}} c2_2^+$

Message board assumption

$$\frac{\varphi : \square_i \varphi}{\square_i \varphi}$$



* Running example from the paper

Relational representation

Sightings_INTERNAL

| tid | sid | uid | species | date | location |
|------|-----|-------|------------|----------|-------------|
| s1.1 | s1 | Carol | Bald eagle | 06-14-08 | Lake Forest |
| s1.2 | s1 | Carol | Fish eagle | 06-14-08 | Lake Forest |
| s2.1 | s2 | Alice | Crow | 06-14-08 | Lake Placid |
| s2.2 | s2 | Alice | Raven | 06-14-08 | Lake Placid |

Comments_INTERNAL

| tid | cid | comment | sid |
|------|-----|-----------------------|-----|
| c1.1 | c1 | found feathers | s2 |
| c2.1 | c2 | plain black feathers | s2 |
| c2.2 | c2 | purple-black feathers | s2 |

Sightings_V

| wid | tid | sid | s | e |
|-----|------|-----|---|---|
| #0 | s1.1 | s1 | + | y |
| #1 | s1.1 | s1 | + | n |
| #1 | s2.1 | s2 | + | y |
| #2 | s1.1 | s1 | - | y |
| #2 | s1.2 | s1 | - | y |
| #2 | s2.2 | s2 | + | y |
| #3 | s1.1 | s1 | + | n |
| #3 | s2.1 | s2 | + | n |

E

| wid1 | uid | wid2 |
|------|-------|------|
| #0 | Alice | #1 |
| #0 | Bob | #2 |
| #0 | Carol | #0 |
| #1 | Bob | #2 |
| #1 | Carol | #0 |
| #2 | Alice | #3 |
| #2 | Carol | #0 |
| #3 | Bob | #2 |
| #3 | Carol | #0 |

Comments_V

| wid | tid | cid | s | e |
|-----|------|-----|---|---|
| #1 | c1.1 | c1 | + | y |
| #2 | c2.2 | c2 | + | y |
| #3 | c1.1 | c1 | + | n |
| #3 | c2.1 | c2 | + | y |

D

| wid | d |
|-----|---|
| #0 | 0 |
| #1 | 1 |
| #2 | 1 |
| #3 | 2 |

S

| wid1 | wid2 |
|------|------|
| #1 | #0 |
| #2 | #0 |
| #3 | #1 |

Example Translation of a Belief CQ (BCQ)

Q: Who disagrees with a sighting from '06-14-08' that Alice believes?

BeliefSQL

```
select  U.name, S1.species
from    Users as U,
        BELIEF 'Alice' Sightings as S1,
        BELIEF U.uid not Sightings as S2
where   S1.sid = S2.sid
and     S1.uid = S2.uid
and     S1.species = S2.species
and     S1.date = '06-14-08'
and     S2.date = '06-14-08'
and     S1.location = S2.location
```

```
q(x,y) :- _Alice S+(u,v,y,'06-14-08',z),
          _x S-(u,v,y,'06-14-08',z)
```

Translation into SQL

```
select  E1.uid as uid1, V.tid, V.sid, R.uid, R.species, R.date, R.location, V.s
into    T2
from    E as E1, Sightings_V as V, Sightings_STAR as R
where   E1.wid1=0
and     V.wid=E1.wid2
and     V.tid=R.tid
and     E1.uid='1';

select  E1.uid as uid1, V.tid, V.sid, R.uid, R.species, R.date, R.location, V.s
into    T1
from    E as E1, Sightings_V as V, Sightings_STAR as R
where   E1.wid1=0
and     V.wid=E1.wid2
and     V.tid=R.tid;

select  T1.uid1, T2.species
from    T1 as T1, T2 as T2
where   T1.sid=T2.sid
and     ((T1.s=0 and T1.uid=T2.uid and T1.species=T2.species
and T1.date='6-14-08' and T1.location=T2.location) or
(T1.s=1 and (T1.uid<>T2.uid or T1.species<>T2.species
or T1.date<>'6-14-08' or T1.location<>T2.location)))

and     T2.s=1
and     T2.date='6-14-08';

drop   table T2;
drop   table T1;
```

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Experiments

Size

Relative overhead $\rho := \frac{|R^*|}{n}$ $\rho = O(m^{d_{\max}})$

m ... #users
 d_{\max} ... maximum
depth of belief
annotation

In theory: e.g. 100 users, max. depth 2
 $\rho \rightarrow 10,000$

Experiments: $\rho \rightarrow 21 - 1,009$

Size not limitation of semantics, but of relational implementation!

Time

Depends on type of query (3 types in paper)

Q1: ~0.1 s

Experiments on 10,000 annotations ($\rho = 22.4$):

Q2: ~0.4 s

Q3: ~4.5 s

Considerable speed-up to come!

Inspirations and related work (excerpt)

- Annotations
 - Buneman et al. [ICDT 2001 / ICDT 2007]
 - Bhagwat et al. [VLDBJ 2005], Geerts et al. [ICDE 2006]
 - Srivastava & Velegrakis [SIGMOD 2007]
- Modal logic
 - Fagin et al. [1995]
 - Calvanese et al. [IS 2008]
 - Nguyen [LJ-IGPL 2008]
- Uncertain / incomplete information
 - Sarma et al. [ICDE 2006]
 - Green & Tannen [IEEE Data Eng. 2006]
 - Dalvi & Suciu [PODS 2007]
- Inconsistency / key violations
 - Arenas et al. [PODS 1999]
 - Fuxman et al. [SIGMOD 2005]
- Peer-to-peer computing / collaborative data sharing
 - Bernstein et al. [WebDB 2002]
 - Ives et al. [SIGMOD record 2008]

Conclusions

- Proposed BELIEF databases
 - Goal: manage, curate inconsistent data
- Implementation
 - Logical foundations
 - Relational translation
- Current work
 - making it compact and fast

BACKUP

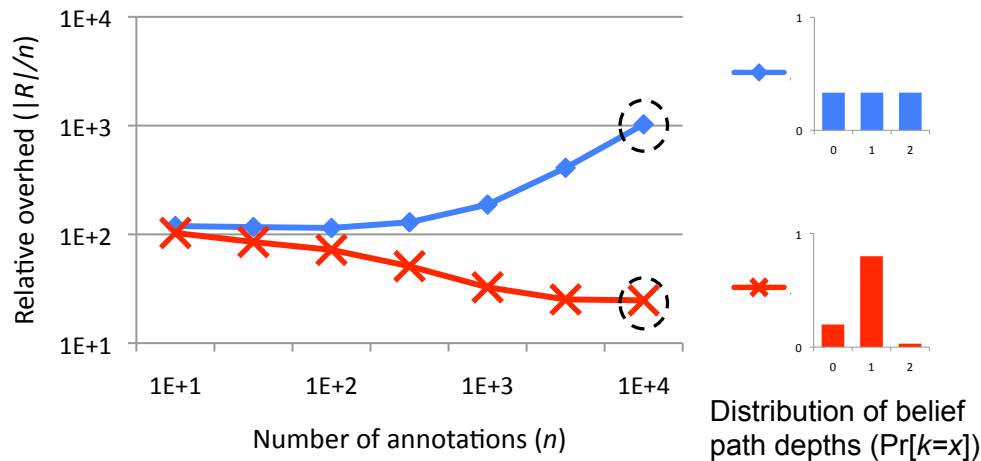
Relative overhead of relational representation

Bound for *relative overhead* $\frac{|\mathcal{R}^*|}{n} = \mathcal{O}(m^{d_{\max}})$

Measured relative overhead $\frac{|\mathcal{R}^*|}{n}$ for $n = 10,000$ annotations, $m = 100$ users, uniform or Zipf user participation, and 3 distributions of annotation depth:

| $\Pr[d = \{0, 1, 2\}]$ | uniform | Zipf |
|------------------------|---------|------|
| $[0.3, 0.3, 0.3]$ | 1,009 | 130 |
| $[0.8, 0.19, 0.01]$ | 162 | 68 |
| $[0.199, 0.8, 0.001]$ | 26 | 21 |

Measured relative overhead $\frac{|\mathcal{R}^*|}{n}$ for $m = 100$ users, uniform user participation, and 2 distributions of annotation depth:



Query types and execution times

1. *Query for content*: “What does Alice believe?” $d \in \{0, \dots, 4\}$:

$$q_{1,d}(x, y) : - \Box_w S^+(x, -, y, -, -), \text{ with } |w| \in \{0, \dots, 4\}$$

2. *Query for conflicts*: “Which animal sightings does Bob believe that Alice believes, which he does not believe himself?”

$$q_2(x, y) : - \Box_{2.1} S^+(x, z, y, u, v), \Box_2 S^-(x, z, y, u, v)$$

3. *Query for users*: Who disagrees with any of Alice’s beliefs of sightings at Lake Placid?”

$$q_3(x) : - \Box_x S^-(y, z, u, v, 'a'), \Box_1 S^+(y, z, u, v, 'a')$$

Execution times and size of result sets for example queries executed over a belief database with 10,000 annotations and relative overhead 22.4.

| | $q_{1,0}$ | $q_{1,1}$ | $q_{1,2}$ | $q_{1,3}$ | $q_{1,4}$ | q_2 | q_3 |
|------------------------|-----------|-----------|-----------|-----------|-----------|-------|-------|
| E(Time) [msec] | 105 | 145 | 146 | 152 | 144 | 436 | 4473 |
| σ (Time) [msec] | 120 | 168 | 153 | 162 | 162 | 186 | 661 |
| Result size | 1626 | 2816 | 2253 | 2061 | 1931 | 196 | 99 |

Belief Conjunctive Queries (BCQ)

Conjunctive Queries (CQ) in Datalog form:

$$q(\bar{x}) :- R_1(\bar{x}_1), \dots, R_g(\bar{x}_g)$$

Belief Conjunctive Queries (BCQ) in "Modal Datalog" form:

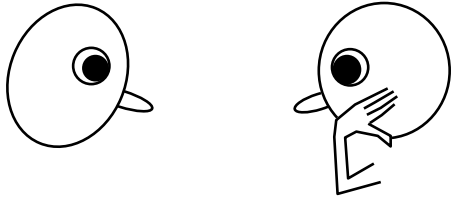
$$q(\bar{x}) :- \Box_{\bar{w}_1} R_1^{s_1}(\bar{x}_1), \dots, \Box_{\bar{w}_g} R_g^{s_g}(\bar{x}_g)$$

q_1 : “*Who disagrees with any sighting from '06-14-08' that Alice believes?*”

$$q_1(x, y) :- \Box_{\text{Alice}} S^+(u, v, y, \text{'06-14-08'}, z), \Box_x S^-(u, v, y, \text{'06-14-08'}, z)$$

$$q_1(D) = \{(\text{'Bob'}, \text{'bald eagle'}), (\text{'Bob'}, \text{'crow'})\}$$

Revisiting the semantics / the user



↓ (3) ?

-> Structured discourse

↓ (2) BeliefSQL

Conflicts in belief worlds:
OWA, keys, ML, DA

↓ (1) SQL

Standard relational model

BELIEF 'Alice' (...,'eagle',...)

-> 'Alice'ASSERTS (...,'eagle',...)

BELIEF 'Bob' BELIEF 'Alice'
(...,'black feathers',...)

-> 'Bob'SUGGESTS that the ASSUMPTION
(...,'black feathers',...) has led 'Alice' to her
original observation